

Description of the algorithm

Conceptually, a merge sort works as follows

Merge sort incorporates two main ideas to improve its runtime:

Example: Using merge sort to sort a list of integers contained in an array:

Suppose we have an array A with n indices ranging from A₀ to A_{n - 1}. We apply merge sort to A(A₀..A_{c - 1}) and A(A_c..A_{n - 1}) where c is the integer part of $n / 2$. When the two halves are returned they will have been sorted. They can now be merged together to form a sorted array.

In a simple pseudocode form, the algorithm could look something like this:

```
function merge_sort(m)
  if length(m) ≤ 1
    return m
  var list left, right, result
  var integer middle = length(m) / 2
  for each x in m up to middle
    add x to left
  for each x in m after middle
    add x to right
  left = merge_sort(left)
  right = merge_sort(right)
  result = merge(left, right)
  return result
```

Following writing merge_sort function, then it is required to merge both the left and right lists created above. There are several variants for the merge() function; one possibility is this:

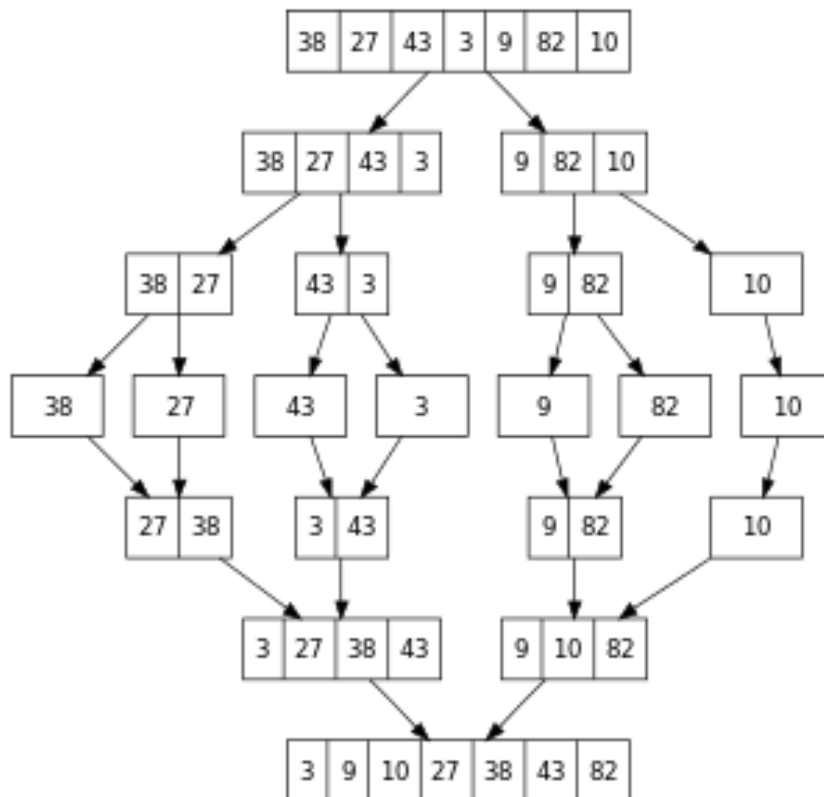
```
function merge(left, right)
  var list result
  while length(left) > 0 or length(right) > 0
    if length(left) > 0 and length(right) > 0
      if first(left) ≤ first(right)
```

```

    append first(left) to result
    left = rest(left)
else
    append first(right) to result
    right = rest(right)
else if length(left) > 0
    append first(left) to result
    left = rest(left)
else if length(right) > 0
    append first(right) to result
    right = rest(right)
end while
return result

```

Marking Scheme



C# code

```
using System;
using System.Collections.Generic;
using System.Linq;
using System.Text;

namespace Merge_Sort
{
    class Program
    {
        /// <summary>
        /// Merge Sort function
        /// </summary>
        /// <param name="input"></param>
        /// <param name="left"></param>
        /// <param name="right"></param>
        public static void Merge_Sort(int[] input, int left, int right)
        {
            if (left < right)
            {
                //calculate middle index of array
                int middle = (left + right) / 2;
                //call function Merge_Sort
                Merge_Sort(input, left, middle);
                Merge_Sort(input, middle + 1, right);

                //Merge
                int[] leftArray = new int[middle - left + 1];
                int[] rightArray = new int[right - middle];
                //copyt array
                Array.Copy(input, left, leftArray, 0, middle - left + 1);
                Array.Copy(input, middle + 1, rightArray, 0, right - middle);

                int indexI = 0;
                int indexJ = 0;

                //loop array
                for (int k = left; k < right + 1; k++)
                {
                    if (indexI == leftArray.Length)
                    {
                        //add value to right
                        input[k] = rightArray[indexJ];
                        indexJ++;
                    }
                    else if (indexJ == rightArray.Length)
                    {
                        //add value to left
                        input[k] = leftArray[indexI];
                        indexI++;
                    }
                    else if (leftArray[indexI] <= rightArray[indexJ])
                    {
                        //add value to left
                        input[k] = leftArray[indexI];
                        indexI++;
                    }
                    else
                    {

```

```

        //add value to right
        input[k] = rightArray[indexJ];
        indexJ++;
    }
}
}
}
/// <summary>
/// Main function
/// </summary>
/// <param name="args"></param>
static void Main(string[] args){
    Console.Write("Enter number of elements: ");
    int max = Convert.ToInt32(Console.ReadLine());
    //array for inputted values
    int[] numbers = new int[max];
    ///prompt user to enter values
    for (int i = 0; i < max; i++){
        Console.Write("Enter [" + (i + 1).ToString() + "] element: ");
        numbers[i] = Convert.ToInt32(Console.ReadLine());
    }
    //show all values
    Console.Write("Array:");
    Console.Write("\n");
    for (int k = 0; k < max; k++)
    {
        //print values
        Console.Write(numbers[k] + " ");
    }

    Console.WriteLine("\n\nArray after Merge Sort");
    //call function Merge Sort
    Merge_Sort(numbers, 0, max - 1);
    for (int i = 0; i < max; i++)
    {
        Console.Write(numbers[i] + " ");
    }
    //delay
    Console.ReadLine();
}
}
}
}

```