

Question #79755, Physics / Classical Mechanics

Mary wants to throw a can straight up into the air and then hit it with a second can. She wants the collision to occur at a height $h=10\text{m}$ above the throw point. In addition she knows that she needs $t_1=4.0\text{s}$ between successive throws. Assume that she throws both cans at the same speed. Take $g=9.81\text{m/s}^2$. Find the initial speed of the cans?

Solution

Let the height of the first can be x , that of the second can be y ; and both cans be thrown at speed v .

$$x(t) = v t - g \frac{t^2}{2}$$

$$y(t) = v (t - t_1) - g \frac{(t - t_1)^2}{2}$$

$$x(t) = y(t) = h$$

From the first height equation:

$$v = \frac{h}{t} + \frac{gt}{2}$$

Substituted into the second equation:

$$h = \left(\frac{h}{t} + \frac{gt}{2} \right) (t - t_1) - \frac{g(t - t_1)^2}{2}$$

$$10 = \left(\frac{10}{t} + 9.81 \frac{t}{2} \right) (t - 4) - \frac{9.81(t - 4)^2}{2}$$

$$t = 4.457 \text{ s.}$$

$$v = \frac{10}{4.457} + \frac{9.81}{2} 4.457 = 24.1 \frac{\text{m}}{\text{s}}.$$

Answer: $24.1 \frac{\text{m}}{\text{s}}$.

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