

Starting from rest at time $t = 0$, a grindstone has a constant angular acceleration of 3.2rad/s^2 . What is the angular displacement after 2.7 s? If the radius of the grindstone is 0.24 m. Calculate the tangential and radial acceleration.

Angular displacement after 2.7 s:

$$\varphi = \frac{\beta t^2}{2}$$
$$\varphi = \frac{3.2\text{rad/s}^2 * (2.7\text{s})^2}{2} = 11.66\text{rad}$$

First of all let's find an angular speed:

$$\omega = \beta t$$

Where β - angular acceleration.

$$\omega = 3.2\text{rad/s}^2 * 2.7\text{s} = 8.64\text{rad/s}$$

Centripetal acceleration:

$$a_n = \omega^2 R = (8.64\text{rad/s})^2 * 0.24\text{m} = 17.92\text{m/s}^2$$

Tangential acceleration:

$$a_t = \beta R$$

$$a_t = 3.2\text{rad/s}^2 * 0.24\text{m} = 0.77\text{m/s}^2$$

Answer: $\varphi = 11.66\text{rad}$, $a_n = 17.92\text{m/s}^2$, $a_t = 0.77\text{m/s}^2$