## Answer on Question \#73658, Physics / Mechanics | Relativity

Question. A small projectile of mass $m$ moves with speed $v$ to the right. The projectiles strikes and sticks to the end of a stationary bar of mass $M$, legth $L$, pivoted about a frictionless axle through its centre. Derive an expression for the angular velocity of the system immediately after the collision.

## Solution.



Using the law of the conservation of angular momentum we get

$$
\frac{m v L}{2}=I \omega,
$$

where I - moment of inertia of the system after interaction.

$$
I=\frac{m L^{2}}{4}+\frac{M L^{2}}{12} .
$$

Hence

$$
\omega=\frac{m v L}{2 I}=\frac{m v L}{2\left(\frac{m L^{2}}{4}+\frac{M L^{2}}{12}\right)}=\frac{m v}{\frac{m L}{2}+\frac{M L}{6}}=\frac{6 m v}{3 m L+M L}=\frac{6 m v}{(3 m+M) L}
$$

Answer. $\omega=\frac{6 m v}{(3 m+M) L}$.

