

Answer on Question #72214-Physics-Other

A guitar string under the tension of 200N, vibrating in its fundamental mode, gives 6 beats/sec. With a tuning fork the player increase the string tension to 242N and again gets 6 beat/sec. Find the frequency of the tuning fork?

Solution

$$f_2 - f = 6 \frac{\text{beat}}{s}.$$

$$f - f_1 = 6 \frac{\text{beat}}{s}.$$

$$\frac{f_2}{f_1} = \sqrt{\frac{T_2}{T_1}}$$

$$\sqrt{\frac{T_2}{T_1}} f_1 - f = 6 \frac{\text{beat}}{s}.$$

$$\sqrt{\frac{T_2}{T_1}} (f - 6) - f = 6.$$

$$\left(\sqrt{\frac{T_2}{T_1}} - 1 \right) f = 6 \left(\sqrt{\frac{T_2}{T_1}} + 1 \right)$$

$$f = 6 \frac{\left(\sqrt{\frac{T_2}{T_1}} + 1 \right)}{\left(\sqrt{\frac{T_2}{T_1}} - 1 \right)} = 6 \frac{\left(\sqrt{\frac{242}{200}} + 1 \right)}{\left(\sqrt{\frac{242}{200}} - 1 \right)} = 126 \text{ Hz}.$$

Answer: 126 Hz.