Question. The critical angle for the material of a prism is 45° and its refracting angle is 30°. A monochromatic ray goes out perpendicular to the surface of emergence from the prism. Then the angle of incidence on the prism will be

Given. $\alpha = 30^\circ$; $\theta_c = 45^\circ$.

Find. β .

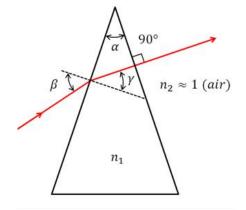
Solution.

Using the equation for the critical angle

we get

$$\theta_c = \arcsin\left(\frac{n_2}{n_1}\right)$$

$$45^\circ = \arcsin\left(\frac{1}{n_1}\right) \rightarrow n_1 = \frac{1}{\sin 45^\circ} = \sqrt{2}.$$



From the figure

 $\gamma = \alpha$.

So

$$\frac{\sin\beta}{\sin\gamma} = \frac{n_1}{n_2} \rightarrow \sin\beta = \frac{n_1 \cdot \sin\gamma}{n_2} \rightarrow$$

$$\beta = \arcsin\left(\frac{n_1 \cdot \sin\gamma}{n_2}\right) = \arcsin\left(\frac{\sqrt{2} \cdot \sin 30^\circ}{1}\right) = \arcsin\left(\frac{\sqrt{2}}{2}\right) \rightarrow$$

 $\beta = 45^{\circ}$

Answer. $\beta = 45^{\circ}$.