

Answer on Question #71096, Physics / Astronomy | Astrophysics

Question: Galaxy NGC2300 has an flat disk dominating the visible light image. Surface brightness is given by the exponential law $I(R) = I_0 \exp(-R/R_d)$ where I_0 is the central surface brightness, R distance from the center, and $R_d = 4$ kpc the exponential radial scale of the disk (e-folding distance). The total luminosity of the galaxy equals $L = (2.5 \cdot 10^{10})L_{\text{sun}}$ Considering that the total luminosity is surface brightness $I(R)$ integrated over the area of the whole disk from $R = 0$ to $R = \infty$ (not over the radial distance, a mistake some people make!), compute I_0 (in units of $L_{\text{sun}}/\text{pc}^2$)

Solution:

$$L = \int_0^{\infty} I_0 e^{-\frac{r}{r_d}} 2\pi r dr = 2\pi I_0 \int_0^{\infty} e^{-\frac{r}{r_d}} r dr = 2\pi I_0 r_d^2$$
$$I_0 = \frac{L}{2\pi r_d^2} = 2.5 * \frac{10^{10} L_{\text{sun}}}{3.14 * 2 * 16 * 10^6 \text{pc}^2} = 248 \frac{L_{\text{sun}}}{\text{pc}^2}$$

Answer:

$$I_0 = 248 \frac{L_{\text{sun}}}{\text{pc}^2}$$

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