69866, Physics / Electromagnetism

Question Two charges lie in a line along the x axis. Charge 1 is q1 = 1.1 C and charge 2 is q2 = 2.5 C. They are each a distance of d = 0.061 m from the origin. What is the distance on the x-axis from the origin at which the electric field will be zero. Give your answer in meters.

Solution The electric field is sum of fields from both charges

$$E = E_1 + E_2 = k\frac{q_1}{r_1^2} - k\frac{q_2}{r_2^2} = 0$$

The signs of E_1 and E_2 are different as they are on different sides of point, where there is no field. Let us suppose it is at distance x from origin. Then

$$\begin{aligned} k\frac{q_1}{r_1^2} &= k\frac{q_2}{r_2^2} \\ \frac{q_1}{(r-x)^2} &= \frac{q_2}{(r+x)^2} \end{aligned}$$

where r = 0.061. Then we can find x:

$$q_2(r^2 - 2xr + x^2) = q_1(r^2 + 2xr + x^2)$$
$$x^2(q_2 - q_1) - 2rx(q_2 + q_1) + r^2(q_2 - q_1) = 0$$
$$1.4x^2 - 2 \cdot 3.6 \cdot 0.061x + 0.061^2 \cdot 1.4 = 0$$

Solving this quadratic equation we find that suiting solution is

$$x = 0.01237$$