

Answer to Question #68962

Question: Find the shortest length L for a steel column with pinned ends having a cross sectional area of 60×100 mm, for which the elastic Euler formula applies. Let $E = 200$ GPa and assume proportional limit to be 250 MPa

$$a = 60\text{mm} = 0.06\text{m}$$

$$b = 100\text{mm} = 0.1\text{m}$$

$$\sigma_c = 250\text{MPa} = 250 * 10^6\text{Pa}$$

$K = 1$ – column effective lengths factor for a 2 side pinned case

Solution: The critical force load on the column

$$F = S\sigma_c = ab\sigma_c$$

On the other hand

$$F = \frac{\pi^2 EI}{(KL)^2}$$

Where I is minimum area moment of inertia of the cross section of the column, in our case

$$I = \frac{a^3 b}{12}$$

In the end

$$ab\sigma_c = \frac{\pi^2 E \frac{a^3 b}{12}}{(KL)^2} \rightarrow L = \frac{\pi^2 E a^2}{12\sigma_c} = 2.37\text{m}$$

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