

Answer on Question #68664, Physics / Mechanics | Relativity

Grains of fine California beach sand are approximately spheres with an average radius of $50\text{ }\mu\text{m}$ and are made of silicon dioxide, which has a density of $2.3 \times 10^3\text{ kg/m}^3$. What mass of sand grains would have a total surface area (the total area of all the individual spheres) equal to the surface area of a cube 0.9 m on an edge?

Solution

$$\begin{aligned}r &= 50\mu\text{m} \\ \rho &= 2.3 \cdot 10^3\text{ kg} \cdot \text{m}^{-3} \\ a &= 0.9\text{m}\end{aligned}$$

Surface of the cube is made of 6 squares. Cube surface area is

$$S = 6a^2 = 6 \cdot 0.9 \cdot 0.9 = 4.86(\text{m}^2)$$

Surface area of a grain of sand is

$$s = 4\pi r^2 = 3,14 \cdot 10^{-8}\text{m}^2.$$

Number of grains which have the same total surface area as the surface area of a cube is

$$N = \frac{S}{s} = 1.55 \cdot 10^8$$

Mass of a grain is

$$m_0 = \rho \cdot \frac{4}{3}\pi r^3 = 1.20 \cdot 10^{-9}\text{kg}$$

Total mass is $m = m_0 N = 0.186\text{kg}$

Answer: 0.186 kg

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