

Answer on Question #68497 – Physics – Mechanics | Relativity

A dock side container crane can lift a fully loaded container of mass 37000 kg from rest to a maximum velocity of 1.2 ms^{-1} in a distance of 8 m . If the friction resistance of the crane winch gear is 2 kN and assuming the acceleration is uniform, determine using the principle of conservation of energy:

- i. work done
- ii. the tension in the lifting cable
- iii. the maximum power developed

Solution.

We find the acceleration of the container:

$$a = \frac{v^2 - v_0^2}{2s} = \frac{1.2^2 - 0}{2 * 8} = \frac{1.44}{16} = 0.09 \text{ ms}^{-2};$$

The Newton's second law for the motion of a container (in projection on the vertical y-axis):

$$m * a = F_1 - mg; F_1 \text{ is the tension in the lifting cable}$$

$$F_1 = m(a + g) = 37000 * (9.81 + 0.09) = 366300 \text{ N} \approx 366 \text{ kN};$$

We find the maximum power developed using the principle of conservation of energy.

$$P = F * v = (F_1 + F_2) * v = (366300 + 2000) * 1.2 = 441960 \text{ W} \approx 442 \text{ kW}; F_2 \text{ is the friction resistance of the crane.}$$

Answer:

ii. $F_1 \approx 366 \text{ kN};$

iii. $P \approx 442 \text{ kW}$