Answer on Question # 68393-Physics / Quantum Mechanics

Suppose that the momentum of a certain particle can be measured to an accuracy of one part in a thousand, Determine the minimum uncertainty in the position of a particle if the particle is (a) a 5 x 10^-3 kg mass moving with a speed of 2 m/s, (b) an electron moving with a speed of 1.8 x 10^8 m/s.

Solution

a) The momentum of the particle $p = mv = 5 \times 10^{-3} \times 2 = 1 \times 10^{-2} \text{ kg} \cdot \frac{\text{m}}{\text{s}}$.

So uncertainty in the momentum of a particle $\Delta p = \frac{1}{1000}p = 1 \times 10^{-5} \text{ kg} \cdot \frac{\text{m}}{\text{s}}$.

From the Heisenberg's uncertainty principle

$$\Delta p \Delta x \ge \frac{\hbar}{2}$$

the minimum uncertainty in the position of a particle

$$\Delta x = \frac{\hbar}{2\Delta p} \approx \frac{1 \times 10^{-34}}{2 \times 10^{-5}} = 5 \times 10^{-28} \,\mathrm{m}$$

b) The momentum of the relativistic electron

$$p = \frac{mv}{\sqrt{1 - \frac{v^2}{c^2}}} = \frac{9.1 \times 10^{-31} \times 1.8 \times 10^8}{\sqrt{1 - \frac{(1.8 \times 10^8)^2}{(3 \times 10^8)^2}}} = \frac{16.38 \times 10^{-23}}{0.8} \approx 2 \times 10^{-22} \,\mathrm{kg} \cdot \frac{\mathrm{m}}{\mathrm{s}}$$
$$\Delta p = \frac{1}{1000} p = 2 \times 10^{-25} \,\mathrm{kg} \cdot \frac{\mathrm{m}}{\mathrm{s}}.$$

Finally

$$\Delta x = \frac{\hbar}{2\Delta p} \approx \frac{1 \times 10^{-34}}{4 \times 10^{-25}} = 2.5 \times 10^{-10} \text{ m} = 2.5 \text{ Å}.$$

Answer a) 5×10^{-28} m, b) 2.5×10^{-10} m.

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