

Answer on Question 68229, Physics, Mechanics | Relativity

Question:

A clock is regulated by a second's pendulum keeps correct time. During summer the length of the pendulum increases by 0.01 meters. How much the clock will lose or gain in one day?

Solution:

Let's first find the period of the pendulum from the formula:

$$T = 2\pi \sqrt{\frac{L}{g}},$$

here, T is the period of the pendulum, L is the length of the pendulum and g is the acceleration due to gravity.

As we know, the length of the second's pendulum is equal to 1.0 m and its period is equal to 2.0 s. Therefore, during the summer the length of the pendulum increases to $L = 1.0 \text{ m} + 0.01 \text{ m} = 1.01 \text{ m}$. Then, substituting the length of the pendulum into the formula above, we get:

$$T = 2\pi \sqrt{\frac{L}{g}} = 2\pi \cdot \sqrt{\frac{1.01 \text{ m}}{9.8 \frac{\text{m}}{\text{s}^2}}} = 2.017 \text{ s}.$$

As we can see from the calculations, the pendulum clock will lose its period. Let's calculate the loss in period:

$$\text{loss} = T_{\text{final}} - T_{\text{initial}} = 2.017 \text{ s} - 2.0 \text{ s} = 0.017 \text{ s}.$$

Finally, we can calculate the loss in period per day:

$$\Delta T = \frac{24 \text{ h} \cdot \frac{3600 \text{ s}}{1 \text{ h}} \cdot 0.017 \text{ s}}{2.017 \text{ s}} = 728.21 \text{ s}.$$

Answer:

$$\Delta T = 728.21 \text{ s}.$$