

Answer on Question #67636, Physics / Atomic and Nuclear Physics

An electron is confined to a one-dimensional region in which its ground-state ($n = 1$) energy is 2.00 eV. (a) What is the length of the region? (b) How much energy is required to promote the electron to its first excited state?

Find: $a - ? \Delta E - ?$

Given:

$$n_1=1$$

$$n_2=2$$

$$E_1=2.00 \text{ eV}=2.00 \times 1.6 \times 10^{-19} \text{ J}$$

$$m=9.10 \times 10^{-31} \text{ kg}$$

$$h=6.63 \times 10^{-34} \text{ J}\cdot\text{s}$$

Solution:

Energy of electron:

$$E_n = \frac{h^2}{8a^2m} n^2 \quad (1)$$

$$\text{Of (1)} \Rightarrow a = \sqrt{\frac{h^2 n_1^2}{8Em}} \quad (2)$$

$$\text{Of (2)} \Rightarrow a=0.4 \times 10^{-9} \text{ m}$$

$$\text{Of (1)} \Rightarrow \Delta E = \frac{h^2}{8a^2m} (n_2^2 - n_1^2) \quad (3)$$

$$\text{Of (3)} \Rightarrow \Delta E=11.32 \times 10^{-19} \text{ J}$$

$$1 \text{ eV} - 1.6 \times 10^{-19} \text{ J}$$

$$\Delta E - 11.32 \times 10^{-19} \text{ J}$$

$$\Delta E=7 \text{ eV}$$

Answer:

$$(a) 0.4 \times 10^{-9} \text{ m}$$

$$(b) 7 \text{ eV}$$