

Answer on Question #67517-Physics-Mechanics-Relativity

An ideal monatomic gas undergoes an adiabatic compression from state 1 with pressure $p_1=1$ atm, volume $V_1=8$ L, and temperature $T_1=300$ K to state 2 with pressure $p_2=32$ atm, volume $V_2=1$ L.

- (a) What is the temperature of the gas in state 2?
- (b) How many moles of gas are present?
- (c) What is the average translational kinetic energy per mole before and after the compression?
- (d) What is the ratio of the squares of the rms speeds before and after the compression?
- (e) If we do not know that the ideal gas here is monatomic, demonstrate that the gas is truly monatomic.

Solution

(a)

$$T_2 = T_1 \frac{p_2 V_2}{p_1 V_1} = 300 \frac{32}{1} \frac{1}{8} = 1200 \text{ K.}$$

(b)

$$n = \frac{p_1 V_1}{RT_1} = \frac{101325 \cdot 0.008}{8.31 \cdot 300} = 0.325 \text{ mol.}$$

(c)

$$K_{before} = \frac{3}{2} k T_1 = \frac{3}{2} (1.38 \cdot 10^{-23}) (300) = 6.21 \cdot 10^{-21} \text{ J.}$$

$$K_{after} = \frac{3}{2} k T_2 = \frac{3}{2} (1.38 \cdot 10^{-23}) (1200) = 2.48 \cdot 10^{-20} \text{ J.}$$

(d) The ratio of the squares of the rms speeds before and after the compression is

$$\frac{T_1}{T_2} = \frac{300}{1200} = \frac{1}{4}.$$

(e) The adiabatic constant is

$$\gamma = \frac{\ln \frac{p_1}{p_2}}{\ln \frac{V_2}{V_1}} = \frac{\ln \frac{1}{32}}{\ln \frac{1}{8}} = \frac{5}{3}.$$

The adiabatic constant for monoatomic gas is

$$\gamma = \frac{C_p}{C_V} = \frac{\frac{5}{2}}{\frac{3}{2}} = \frac{5}{3}.$$

Thus, the gas is monoatomic.