

Calculate the drift velocity and mean free path of copper when it carries a steady current of 10 amperes and whose radius is 0.08 cm. Assume that the mean thermal velocity = 1.6×10^6 m/s and the resistivity of copper = 2×10^{-8} ohm m

Answer:

The current density is electric current per unit area, $J=I/A$

$$J = nev_d \quad \begin{array}{l} n = \text{free electron density} \\ v_d = \text{drift velocity} \end{array}$$

$$n = \frac{\text{Avogadro's number} \quad \text{Density}}{\text{Atomic mass}} = \frac{(N_A \text{ atoms / mole})(\rho \text{ kg / m}^3)}{A(\text{kg / mole})}$$

For copper:

$$n = \frac{(6.02 \times 10^{23} \text{ atoms / mole})(8.92 \times 10^3 \text{ kg / m}^3)}{63.5 \times 10^{-3} \text{ kg / mole}} = 8.46 \times 10^{28} / \text{m}^3$$

The mean free path of an electron in copper under these conditions can be calculated from

$$d = \frac{m V_t}{n \rho e^2} = \frac{9.11 \cdot 10^{-31} 1.6 \times 10^6}{8.46 \cdot 10^{28} 2 \times 10^{-8} (1.6 \cdot 10^{-19})^2} = 3.4 \cdot 10^{-8} \text{ m}$$

The drift velocity

$$V_d = \frac{I}{\pi r^2 n e} = \frac{10}{3.14 (8 \cdot 10^{-4})^2 8.46 \cdot 10^{28} 1.6 \cdot 10^{-19}} = 0.0015 \frac{\text{m}}{\text{s}}$$