Answer on Question #66741-Physics-Mechanics-Relativity

A proton undergoes a head on elastic collision with a particle of unknown mass which is initially at rest and rebounds with 16/25 of its initial kinetic energy. Calculate the ratio of the unknown mass with respect to the mass of the proton.

Solution

From the conservation of energy:

$$E_{p} = E'_{p} + E$$

$$\frac{16}{25}E_{p} = E'_{p}$$

$$\left(\frac{v'}{v}\right)^{2} = \frac{16}{25} \to \frac{v'}{v} = \frac{4}{5}.$$

$$\frac{25 - 16}{25}E_{p} = E$$

$$\frac{mV^{2}}{m_{p}v^{2}} = \frac{9}{25} \to \frac{m}{m_{p}} = \frac{9}{25}\frac{v^{2}}{V^{2}}.$$

From the conservation of momentum:

$$m_p v = mV - m_p v'$$

$$V = \frac{m_p}{m} (v + v') = \frac{m_p}{m} \left(v + \frac{4}{5} v \right) = \frac{9}{5} v \frac{m_p}{m}$$

Thus,

$$\frac{m}{m_p} = \frac{9}{25} \left(\frac{m}{m_p}\right)^2 \frac{25}{81} = 9 \left(\frac{m}{m_p}\right)^2$$

$$\frac{m}{m_p} = \frac{1}{9}$$

Answer: $\frac{1}{9}$.