

A square prism of wood 50*50 mm in cross section and 300 mm long is subjected to a tensile stress of 4 t/cm² along its longitudinal axis and lateral compressive to a tensile stress of 2 t/cm² along one pair of sides and a lateral tensile stress of 1.0 t/cm² acting along the other pair of sides. If the value of E of the material is 1.5*10⁵ kg/cm², calculate its changed dimensions. Poisson's ratio for wood = 0.4

Let

$$\left\{ \begin{array}{l} l_x = l_y = 50 \text{ mm}, l_z = 300 \text{ mm} \\ \sigma_x = 2000 \frac{\text{kg}}{\text{cm}^2}, \sigma_y = 1000 \frac{\text{kg}}{\text{cm}^2}, \sigma_z = 4000 \frac{\text{kg}}{\text{cm}^2} \\ E = 1.5 \cdot 10^5 \frac{\text{kg}}{\text{cm}^2} \end{array} \right.$$

$$\sigma = E \frac{\Delta l}{l} \rightarrow \Delta l = \frac{\sigma l}{E}$$

$$\left\{ \begin{array}{l} \rightarrow \Delta l_x = \frac{\sigma_x l}{E} = 2000 \cdot \frac{0.5}{1.5 \cdot 10^5} = 666 \cdot 10^{-5} \text{ cm} \\ \rightarrow \Delta l_y = \frac{\sigma_y l}{E} = 1000 \cdot \frac{0.5}{1.5 \cdot 10^5} = 333 \cdot 10^{-5} \text{ cm} \\ \rightarrow \Delta l_z = \frac{\sigma_z l}{E} = 4000 \cdot \frac{30}{1.5 \cdot 10^5} = 666 \cdot 10^{-5} = 0.8 \text{ cm} \end{array} \right.$$

$$\left\{ \begin{array}{l} \rightarrow L_x = l_x + \Delta l_x = 0.5 + 666 \cdot 10^{-5} \text{ cm} \\ \rightarrow L_y = l_y + \Delta l_y = 0.5 + 333 \cdot 10^{-5} \text{ cm} \\ \rightarrow L_z = l_z + \Delta l_z = 3.8 \text{ cm} \end{array} \right.$$