

Answer on Question #65592-Mechanics - Relativity

A solid cylinder of mass $m = 3.0$ kg and radius $r = 1.0$ m is rotating about its axis with a speed of $\omega = 40$ rad s⁻¹. Calculate the torque which must be applied to bring it to rest in $t = 10$ s. What would be the power required?

Solution

The second Newton's law for rotation

$$J \frac{\Delta\omega}{\Delta t} = M.$$

Here $J = \frac{mr^2}{2} = \frac{3 \times 1^2}{2} = 1.5$ kg · m² is the moment of inertia, $\Delta\omega = \omega - \omega_0 = 0 - 40 = -40$ $\frac{\text{rad}}{\text{s}}$.

So the torque

$$M = J \frac{\Delta\omega}{\Delta t} = 1.5 \frac{-40}{10} = -6 \text{ N} \cdot \text{m}.$$

The work done is equal the change in kinetic energy

$$W = \Delta E = \frac{J\omega^2}{2} - \frac{J\omega_0^2}{2} = 0 - \frac{1.5 \times 40^2}{2} = -1200 \text{ J}.$$

The power required

$$P = \frac{W}{t} = \frac{1200}{10} = 120 \text{ W}.$$

Answer $M = 6 \text{ N} \cdot \text{m}$, $P = 120 \text{ W}$.