

Answer on Question #65269 –Physics - Molecular Physics - Thermodynamics

Condition:

Question 01:

2.0g of Nitrogen gas is at 270C in a fixed volume. If 20% of its total internal energy is due to rotation what is the average velocity of nitrogen molecules?

What will be the temperature 2.0 g of Helium gas in a fixed volume if the average velocity of its molecules is 20 m/s ?

Plot schematic of Cv v/s T curve based for nitrogen and helium gas based on Kinetic theory.

Question 02:

200g of melting ice is introduced to a huge lake at 270C. Find the total entropy change of ice-lake system.

200g of melting ice is introduced to a huge lake at 0.20C. Find the total entropy change of ice-lake system.

Can you draw any conclusion based on result? (Hint: tends to reversible, irreversible etc)

Solution:

Question 01:

Nitrogen gas is diatomic gas so N_2 has 5 degrees of freedom so total internal energy is $U = \frac{5}{2}kT * N$, where k is Boltzmann constant ($k=1.38 \times 10^{-23} \text{ J/K}$), $T=270\text{C} = 543 \text{ K}$, N is quantity of molecules.

$N = \frac{m}{M} N_A$, where m=2.0g , M is molar mass(Molecular Weight):

$M(N_2) = 28 \frac{g}{mol}$, N_A is Avogadro constant ($N_A = 6,023 * 10^{23} \text{ mol}^{-1}$).

$$N = \frac{2}{28} * 6,023 * 10^{23} = 0,43 * 10^{23} = 4,3 * 10^{22}$$

$$U = \frac{5}{2} * 1,38 * 10^{-23} * 543 * 4,3 * 10^{22} = 805,54 \text{ J}$$

If 20% of its total internal energy is due to rotation then 80% is the average energy of motion:

$$E = 0,8 * 805,54 = 644,4 \text{ J}$$

On the other hand: $= N * E_0$, where N is quantity of molecules and E_0 is kinetic energy of one molecule.

$$E_0 = \frac{E}{N} = \frac{644,4}{4,3 * 10^{22}} = 149,86 * 10^{-22} = 1,5 * 10^{-20} \text{ J}$$

On the other hand: $E_0 = m_0 \frac{v^2}{2}$, where v is the average velocity, m_0 - molecular mass:

$$m_0 = 28 * 1,66 * 10^{-27} = 4,65 * 10^{-26} \text{ kg}$$

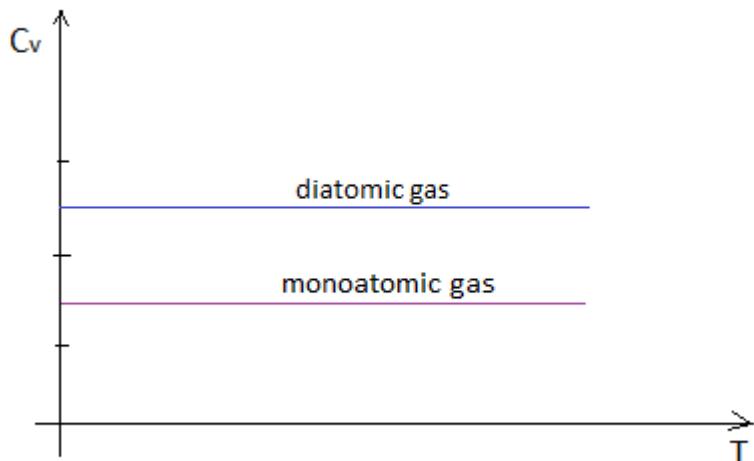
$$V = \left(\frac{2E_0}{m_0} \right)^{1/2} = \left(\frac{2 * 1,5 * 10^{-20}}{4,65 * 10^{-26}} \right)^{1/2} = (0,645 * 10^6)^{1/2} = 0,803 * 10^3 \frac{m}{s} = 803 \frac{m}{s}$$

Helium gas is monoatomic gas so $E_0 = \frac{3}{2} kT = m_0 \frac{V^2}{2} \rightarrow T = m_0 \frac{V^2}{3k}$

$$m_0 = 4 * 1,66 * 10^{-27} = 6,64 * 10^{-27} \text{ kg}$$

$$T = 6,64 * 10^{-27} * \frac{20^2}{3 * 1,38 * 10^{-23}} = 641,5 * 10^{-4} \text{ K} = 0,064 \text{ K} = -273,086 \text{ C}$$

$$C_v = \frac{\delta Q}{\delta T} = \frac{\delta U}{\delta T} \rightarrow C_v(N_2) = \frac{\delta(\frac{5}{2}kT)}{\delta T} = \frac{5}{2}k ; C_v(He) = \frac{\delta(\frac{3}{2}kT)}{\delta T} = \frac{3}{2}k$$



Question 02:

a) Ice->water->steam:

Heat of fusion for ice: $q=335 \text{ kJ/kg}$. Warmth which is necessary for ice thawing: $Q = q * m = 335 * 0,2 = 67 \text{ kJ}$.

$$\Delta S_1 = \frac{Q}{T_0} = \frac{67}{273} = 0,245 \frac{\text{kJ}}{\text{K}} = 245 \frac{\text{J}}{\text{K}}$$

Heat capacity for water: $c=4,187 \text{ kJ/kg*K}$. Warmth which is necessary for heating water from $T_0 = 0\text{C}$ (273K) to $T=100\text{C}$ (373 K):

$$Q = c * m * (T - T_0) = 4,187 * 0,2 * 100 = 83,74 \text{ kJ}$$

$$\Delta S_2 = Q * \ln \frac{T}{T_0} = 83,74 * \ln \left(\frac{373}{273} \right) = 25959 \frac{J}{K}$$

Heat of vaporization for water: $L=2260 \text{ kJ/kg}$. Warmth which is necessary for water vaporization $Q = Lm = 2260 * 0,2 = 452 \text{ kJ}$.

$$\Delta S_3 = \frac{Q}{T} = \frac{452}{373} = 1211,8 \frac{J}{K}$$

Heat capacity for steam: $c=2 \text{ kJ/kg*K}$. Warmth which is necessary for heating steam from $T = 100\text{C}$ (373K) to $T_1=270\text{C}$ (543 K):

$$Q = c * m * (T_1 - T) = 2 * 0,2 * 170 = 68 \text{ kJ}$$

$$\Delta S_4 = Q * \ln \frac{T_1}{T} = 68 * \ln \left(\frac{543}{373} \right) = 29172 \frac{J}{K}$$

$$\Delta S = 245 + 25959 + 1211,8 + 29172 = 56587,8 \frac{J}{K} \text{ - entropy change for ice.}$$

The lake loses warmth: $Q=-(67+83,74+452+543)=-1145,74 \text{ kJ}$. But temperature of the *large* lake is a constant so entropy change for lake: $\Delta S = \frac{Q}{T} = \frac{-1145,74}{543} = -2110 \frac{J}{K}$

$$\text{The total entropy change of ice-lake system: } \Delta S = 56587,8 + (-2110) = 54477,8 \frac{J}{K}$$

b) Heat of fusion for ice: $q=335 \text{ kJ/kg}$. Warmth which is necessary for ice thawing: $Q = q * m = 335 * 0,2 = 67 \text{ kJ}$. $\Delta S_1 = \frac{Q}{T_0} = \frac{67}{273} = 0,245 \frac{kJ}{K} = 245 \frac{J}{K}$

Heat capacity for water: $c=4,187 \text{ kJ/kg*K}$. Warmth which is necessary for heating water from $T_0 = 0\text{C}$ (273K) to $T=0,2\text{C}$ (273,2 K): $Q = c * m * (T - T_0) = 4,187 * 0,2 * 0,2 = 0,167 \text{ kJ}$

$$\Delta S_2 = Q * \ln \frac{T}{T_0} = 0,167 * \ln \left(\frac{273,2}{273} \right) = 0,12 \frac{J}{K}$$

$$\Delta S = \Delta S_1 + \Delta S_2 = 245,12 \frac{J}{K} \text{ - entropy change for ice.}$$

The lake loses warmth: $Q=-(67+0,12)=-67,12 \text{ kJ}$. But temperature of the *large* lake is a constant so entropy change for lake: $\Delta S = \frac{Q}{T} = \frac{-67,12}{273,2} = -245,68 \frac{J}{K}$

$$\text{The total entropy change of ice-lake system: } \Delta S = 245,12 + (-245,68) = -0,56 \frac{J}{K}$$

If we don't take in attention of heating of water then the total entropy change of ice-lake system is $0 \frac{J}{K}$.

The total entropy of an isolated system always increases over time therefore it is irreversible process.

Answer:

Question 01: average velocity of nitrogen molecules is $803 \frac{m}{s}$; temperature of Helium gas is $0,064 K = -273,086 C$

Question 02: The total entropy change of ice-lake system is $54477,8 \frac{J}{K}$ and $0 \frac{J}{K}$