

**Answer on** Question #65231, Physics / Optics

Two energy levels of an atomic system are separated by energy corresponding to frequency  $3.0 \times 10^{14}$  Hz. Assume that all atoms are in one or the other of these two energy levels, compute the fraction of atoms in the upper energy level at temperature 400 K. Take  $k = 1.38 \times 10^{-23} \text{JK}^{-1}$  and  $h = 6.6 \times 10^{-34} \text{Js}$ .

**Find:**  $\frac{N_2}{N_1} - ?$

**Given:**

$$\Delta u = 3.0 \times 10^{14} \text{ Hz}$$

$$T = 400 \text{ K}$$

$$k = 1.38 \times 10^{-23} \text{ J} \times \text{K}^{-1}$$

$$h = 6.6 \times 10^{-34} \text{ J} \times \text{s}$$

**Solution:**

Boltzmann factor:

$$\frac{N_2}{N_1} = \exp \frac{E_1 - E_2}{kT} \quad (1), \text{ where level 2 (N}_2\text{) is higher than level 1 (N}_1\text{)}$$

Energy difference:

$$E_1 - E_2 = h\Delta u \quad (2)$$

$$(2) \text{ in } (1): \frac{N_2}{N_1} = \exp \frac{h\Delta u}{kT} \quad (3)$$

$$\text{Of } (3) \Rightarrow \frac{N_2}{N_1} = \exp \frac{6.6 \times 10^{-34} \times 3.0 \times 10^{14}}{1.38 \times 10^{-23} \times 400} = \exp^{-35.9} \approx 0$$