

Answer on Question #63816-Physics-Other

Show that any solution of the Dirac equation is also a solution of the Klein-Gordon (KG) equation.

Solution

Let ψ is a solution of the Dirac equation:

$$(-\gamma^0 p^0 + \gamma^j p^j + mc)\psi(x) = 0$$

Multiply this equation by $(\gamma^0 p^0 - \gamma^j p^j + mc)$:

$$(\gamma^0 p^0 - \gamma^j p^j + mc)(-\gamma^0 p^0 + \gamma^j p^j + mc)\psi(x) = 0$$

$$((\vec{p})^2 - (p^0)^2 + m^2 c^2)\psi(x) = 0, \quad \text{where } p^0 = \frac{E}{c}$$

Therefore, ψ is a solution of the Klein-Gordon equation.