

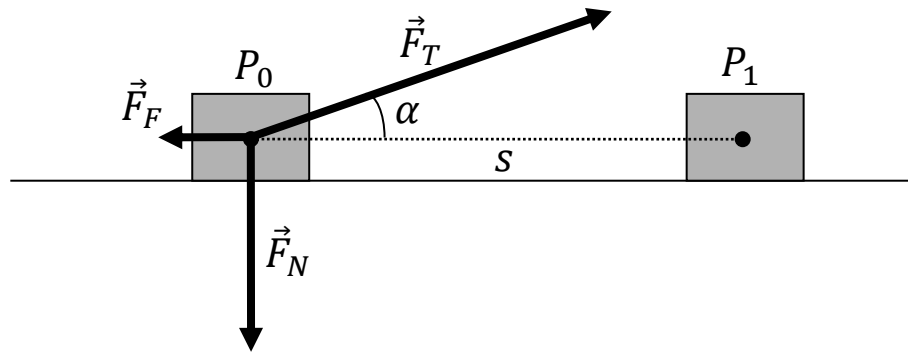
Answer on Question #63514, Physics / Mechanics | Relativity

Question:

Susan's 11.0 kg baby brother Paul sits on a mat. Susan pulls the mat across the floor using a rope that is angled 30° above the floor. The tension is a constant 30.0 N and the coefficient of friction is 0.180.

Use work and energy to find Paul's speed after being pulled 3.10 m.

Solution:



Let us assume that the weight of the mat is negligibly small. To use work and energy we must consider horizontal components of forces acting on Paul.

$$F_T^x = F_T \cdot \cos \alpha$$

$F_F^x = kF_N = kmg$, where k is the coefficient of friction, m is the mass of Paul and g is the gravitational acceleration.

$$\text{The resultant force } F_{res} = F_T \cdot \cos \alpha - kmg$$

$$\text{The work of this force } W = (F_T \cdot \cos \alpha - kmg) \cdot s$$

Kinetic energy at the point P_1 is calculated as $E_k = \frac{mv^2}{2}$, and according to the law of conservation of energy $W = E_k$ or $(F_T \cdot \cos \alpha - kmg) \cdot s = \frac{mv^2}{2}$.

$$\text{Then the speed } v = \sqrt{\frac{2s \cdot (F_T \cdot \cos \alpha - kmg)}{m}}$$

$$v = \sqrt{\frac{2 \cdot 3.1 \cdot (30.0 \cdot \cos 30^\circ - 0.18 \cdot 11.0 \cdot 9.81)}{11.0}} = 1.9 \text{ m/s}$$

Answer:

$$1.9 \text{ m/s}$$