

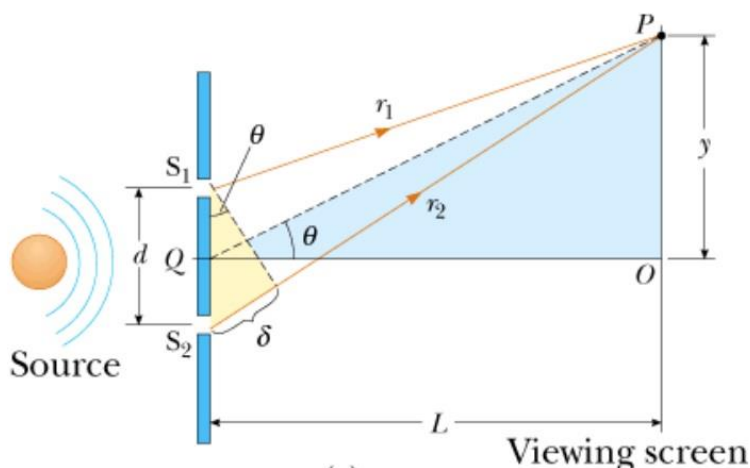
Answer on Question #61774, Physics / Optics

What will be the change in fringe pattern in young double slit experiment even if two mica foils having same refracting indices and thickness L_1 and L_2 ($L_1 > L_2$) are placed in the path of interfering rays

Solution:

Consider the light rays from the two coherent point sources made from *infinitesimal* slits a distance d apart. We assume that the sources are emitting monochromatic light of wavelength λ .

The rays are emitted in all forward directions, but let us concentrate on only the rays that are emitted in a direction θ toward a distant screen (θ measured from the normal to the screen, diagram below). One of these rays has further to travel to reach the screen, and the *path difference* is given by $d \sin \theta$. If this path difference is exactly one wavelength λ or an integer number of wavelengths, then the two waves arrive at the screen in phase and there is constructive interference, resulting in a bright area on the screen.



$$y_{\text{bright}} = \frac{\lambda L}{d} m$$

Our case equal to situation, when a transparent foil of thickness $(L_1 - L_2)$ and refractive index n is placed in one of the incoming wave path, due to the increase of the path by $(n-1)(L_1 - L_2)$, the interference pattern undergoes a shift s .

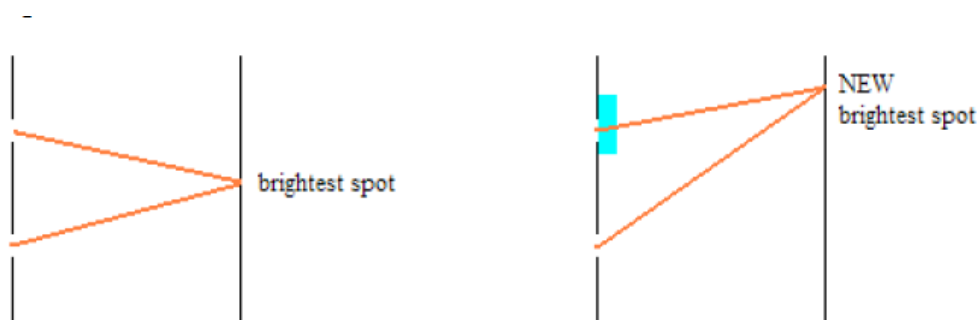


Fig. Equal effective path lengths without (left) and with (right) mica foil.

If the foil has an effective thickness $(L_1 - L_2)$, then there are $\frac{L_1 - L_2}{\lambda/n}$ complete wavelengths that travel through it, while there are $\frac{L_1 - L_2}{\lambda/1}$ wavelengths that travel through the same thickness of air.

The number of fringes shifted is

$$m = \left| \frac{L_1 - L_2}{\lambda/n} - \frac{L_1 - L_2}{\lambda} \right| = \frac{L_1 - L_2}{\lambda} (n - 1)$$

$$\text{Shift of pattern } s = y_{\text{bright}} = \frac{\lambda L}{d} m = \frac{\lambda L}{d} \frac{L_1 - L_2}{\lambda} (n - 1) = \frac{L}{d} (n - 1)(L_1 - L_2).$$

Answer: Due to the increase of the path by $(n-1)(L_1 - L_2)$, the fringe system shifts on the side of the thicker (L_1) mica foil.

<https://www.AssignmentExpert.com>