

### Answer on Question #61299-Physics-Mechanics-Relativity

A satellite of mass  $2.00 \times 10^4$  kg is placed in orbit  $6.00 \times 10^5$  m above the surface of Jupiter.

- Determine the force of gravitational attraction between the satellite and Jupiter.
- What must be the orbital speed of the satellite?
- What must be the value of the gravitational field constant,  $g$ , at the location of the satellite?
- One of the moons of Jupiter is Europa. Its period of motion is  $3.07 \times 10^5$  s. What must be the radius of its orbit?
- If a satellite was placed in orbit around Europa at a height of 100.0 km above the surface of Europa, and the period of motion was  $7.58 \times 10^3$  s, what must be the mass of Europa? The radius of the moon Europa is  $1.57 \times 10^6$  m.

### Solution

a)

$$F = 6.67 \cdot 10^{-11} \frac{(2.00 \cdot 10^4)(1.90 \cdot 10^{27})}{(6.00 \cdot 10^5)^2} = 7.04 \cdot 10^9 \text{ N}$$

b)

$$F = \frac{mv^2}{r}$$

$$v^2 = \frac{Fr}{m}$$

$$v = \sqrt{\frac{Fr}{m}} = \sqrt{6.67 \cdot 10^{-11} \frac{(1.90 \cdot 10^{27})}{6.00 \cdot 10^5}} = 7.60 \cdot 10^5 \frac{\text{m}}{\text{s}}$$

c)

$$g = \frac{F}{m} = 6.67 \cdot 10^{-11} \frac{(1.90 \cdot 10^{27})}{(6.00 \cdot 10^5)^2} = 3.52 \cdot 10^6 \frac{\text{m}}{\text{s}^2}$$

d)

$$T^2 = \left( \frac{4\pi^2}{GM} \right) r^3$$

$$r = \sqrt[3]{\frac{GM}{4\pi^2} T^2} = \sqrt[3]{\frac{(6.67 \cdot 10^{-11})(1.90 \cdot 10^{27})}{4\pi^2} (3.07 \cdot 10^5)^2} = 6.71 \cdot 10^8 \text{ m}$$

e)

$$M = \left( \frac{4\pi^2}{G} \right) \frac{r^3}{T^2} = \left( \frac{4\pi^2}{(6.67 \cdot 10^{-11})} \right) \frac{(1.57 \cdot 10^6 + 1.00 \cdot 10^5)^3}{(7.58 \cdot 10^3)^2} = 4.80 \cdot 10^{22} \text{ kg}$$