

Answer on Question #61087, Physics / Astronomy | Astrophysics

A main sequence star has mass 2×10^{31} kg and radius 3×10^9 m. Obtain an estimate of the average temperature throughout the star.

Find: $T_{\text{star}} - ?$

Given:

$$m_{\text{star}} = 2 \times 10^{31} \text{ kg}$$

$$r_{\text{star}} = 3 \times 10^9 \text{ m}$$

$$m_{\text{sun}} = 1,9891 \times 10^{30} \text{ kg}$$

$$r_{\text{sun}} = 6,96 \times 10^8 \text{ m}$$

$$T_{\text{sun}} = 5778 \text{ K}$$

Solution:

The relationship between luminosity L, temperature T and radius r:

$$L_{\text{star}} = L_{\text{sun}} \left(\frac{r_{\text{star}}}{r_{\text{sun}}} \right)^2 \left(\frac{T_{\text{star}}}{T_{\text{sun}}} \right)^4 \quad (1)$$

$$m = \frac{m_{\text{star}}}{m_{\text{sun}}} \quad (2)$$

$$\text{Of (2)} \Rightarrow m = 10.1$$

$$\text{If } m = 10.1 \text{ (} 2 < m < 20 \text{), then } l = \frac{L_{\text{star}}}{L_{\text{sun}}} = m^{3.5} \quad (3)$$

$$(3) \text{ in (1): } (10.1)^{3.5} = \frac{(3 \times 10^9)^2}{(6,96 \times 10^8)^4} \left(\frac{T_{\text{star}}}{T_{\text{sun}}} \right)^4 \quad (4)$$

$$\text{Of (4)} \Rightarrow \left(\frac{T_{\text{star}}}{T_{\text{sun}}} \right)^4 = 176.23 \quad (5)$$

$$\text{Of (5)} \Rightarrow \frac{T_{\text{star}}}{T_{\text{sun}}} = 3.64 \quad (6)$$

$$\text{Of (6)} \Rightarrow T_{\text{star}} = 21032 \text{ K}$$

Answer:

$$21032 \text{ K}$$