

## Answer on Question 60746, Physics, Atomic and Nuclear Physics

### Question:

Calculate the mass defect and binding energy per nucleon for a lithium nucleus ( ${}^7_3\text{Li}$ ):

Mass of the lithium nucleus  $M = 7.0 u$

Mass of the proton  $m_p = 1.007825 u$

Mass of the neutron  $m_n = 1.008665 u$

$1 u = 1.6605 \cdot 10^{-27} kg = 931 MeV$ .

### Solution:

a) The mass of the nucleus of an atom of any element is always found to be less than the sum of the masses of its constituent nucleons. This difference in mass is called the mass defect. Mathematically it can be written as follows:

$$\Delta m = (Z \cdot m_p + N \cdot m_n) - M,$$

here,  $Z$  is the number of protons,  $N$  is the number of neutrons,  $m_p$  is the mass of the proton,  $m_n$  is the mass of the neutron and  $M$  is the mass of the nucleus of an atom.

Let's substitute the numbers and find  $\Delta m$ :

$$\begin{aligned}\Delta m &= (Z \cdot m_p + N \cdot m_n) - M = (3 \cdot 1.007825 u + 4 \cdot 1.008665 u) - 7.0 u = \\ &= 3.023475 u + 4.03466 u - 7.0 u = 0.058135 u = \\ &= 0.058135 \cdot 1.6605 \cdot 10^{-27} kg = 9.65 \cdot 10^{-29} kg.\end{aligned}$$

b) Let's first use the famous Einstein formula to find the binding energy of the nucleons:

$$\begin{aligned}E &= \Delta mc^2 = [(Z \cdot m_p + N \cdot m_n) - M] \cdot c^2 = \\ &= 0.058135 \cdot 1.6605 \cdot 10^{-27} kg \cdot \left(3.0 \cdot 10^8 \frac{m}{s}\right)^2 = 8.685 \cdot 10^{-12} J = \\ &= 54.28 MeV.\end{aligned}$$

${}^7_3\text{Li}$  has 7 nucleons (3 protons and 4 neutrons). Then, the binding energy per nucleon will be:

$$E_{per\ nucleon} = \frac{E}{A} = \frac{E}{Z + N} = \frac{54.28 MeV}{7} = 7.754 MeV.$$

**Answer:**

a)  $\Delta m = 9.65 \cdot 10^{-29} \text{ kg}$ .

b)  $E_{\text{per nucleon}} = 7.754 \text{ MeV}$ .

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