

Answer on Question 60745, Physics, Other

Question:

An X-ray tube operates at 40 kV. Calculate the minimum wavelength of the emitted rays.

Solution:

There is an inverse relationship between the energy of the emitted rays and its wavelength:

$$E = \frac{hc}{\lambda},$$

here, $h = 6.626 \cdot 10^{-34} \text{ J} \cdot \text{s}$ is the Planck's constant, c is the speed of light, λ is the wavelength of the emitted rays.

From the other hand:

$$E = eU,$$

here, $e = 1.6 \cdot 10^{-19} \text{ C}$ is the charge of the electron, U is the voltage at which the X-ray tube operates.

Then, we can equate these relationships and find the minimum wavelength of the emitted rays:

$$eU = \frac{hc}{\lambda},$$

$$\lambda = \frac{hc}{eU} = \frac{6.626 \cdot 10^{-34} \text{ J} \cdot \text{s} \cdot 3 \cdot 10^8 \frac{\text{m}}{\text{s}}}{1.6 \cdot 10^{-19} \text{ C} \cdot 40 \cdot 10^3 \text{ V}} = 3.1 \cdot 10^{-11} \text{ m}.$$

Answer:

$$\lambda = 3.1 \cdot 10^{-11} \text{ m}.$$