Answer on Question 59027, Physics, Electromagnetism

Question:

From Gauss's law which of the following is not correct:

a) The outward flux of electric field through an enclosed surface is proportional to the electric charges enclosed.

b) The field at a point outside a spherically symmetric charge is the same as the electric field at the same point due to a point charge at its centre.

c) The electric flux through a Gaussian surface is a vector product of the electric field and a unit vector perpendicular to and outward from the surface.

d) The total electric flux through a cylinder placed in an electric field with its axis parallel to the field is zero.

Answer:

The Gauss's law states that the net electric flux through any closed surface is equal to $1/\varepsilon$ times the net electric charge within that closed surface. Gauss's law can be written mathematically as follows:

$$\Phi_E = \frac{Q}{\varepsilon_0},$$

here, Φ_E is the electric flux through a closed surface *S* enclosing any volume *V*, *Q* is the total charge enclosed within *S*, and ε_0 is the permettivity of free space.

The electric flux Φ_E is defined as a surface integral of the electric field:

$$\Phi_E = \oint \boldsymbol{E} \cdot d\boldsymbol{A},$$

here, E is the electric field, dA is the vector representing an infinitesimal element of area of the surface, symbol dot (·) represents the dot product of two vectors.

Finally, we get:

$$\oint \boldsymbol{E} \cdot d\boldsymbol{A} = \frac{Q}{\varepsilon_0}$$

From the definition of the Gauss's law we can see, that the third statement c) is wrong, because there is no vector product in the mathematical definition of the law.