

Answer on Question #57792, Physics – Molecular Physics | Thermodynamics

A student walking to class on a cold day ($T=0\text{ }^{\circ}\text{C}$) finds a silver ring with an inner diameter of $D=1.8\text{ cm}$. The silver has a coefficient of expansion of $\alpha=18.7 \times 10^{-6}$

a) Input an expression for the rings inner diameter D_h when the student warms it up to their body temperature, T_b .

b) What is the change in diameter in mm if $T_b = 37\text{ }^{\circ}\text{C}$

Solution:

a)

The hole in ring expands as if were filled with silver, so the change in the diameter is given by

$$\Delta D = \alpha D_0 \Delta T,$$

where $\alpha = 18.7 \times 10^{-6}$ is the coefficient of linear expansion, D_0 is the original diameter, and ΔT is the change in temperature.

b)

Hence, the change in the ring's diameter is

$$\Delta D = \alpha D_0 \Delta T = (18.7 \cdot 10^{-6})(1.8 \cdot 10^{-2}\text{ m})(37 - 0\text{ }^{\circ}\text{C}) = 12.4542 \cdot 10^{-6}\text{ m} \approx 0.0125\text{ mm}$$

Answer: 0.0125 mm