

Answer on Question#54675, Physics/Mechanics | Kinematics | Dynamics

I) Using formula for sum of two sine functions, obtain:

$$y_1 + y_2 = a \sin(w_1 t - k_1 x) + a \sin(w_2 t - k_2 x) = 2a \sin\left(\frac{(w_1 + w_2)t}{2} - \frac{(k_1 + k_2)x}{2}\right) \cos\left(\frac{(w_1 - w_2)t}{2} - \frac{(k_1 - k_2)x}{2}\right)$$

II) The resulting wave is a sine wave with frequency $\frac{(w_1 + w_2)}{2}$ with enveloping cosine function

of frequency $\frac{w_1 - w_2}{2}$. Because the frequencies of the initial two waves are not equal but almost the same, the enveloping cosine function has a small frequency (big period). This phenomenon is called beats. For equal frequencies of incident waves, the beats do not occur.