

Answer on Question#51505 - Physics - Electromagnetism

1. A voltmeter connected across a 60Hz ac source reads 240V. Write down the expression of the instantaneous voltage as a function of time.
2. An air-cored transformer is assumed to be 100% efficient. The ratio of the secondary turns to the primary turns is 1:20. A 240V ac supply is connected to the primary coil and a 6Ω load is connected to the secondary coil. What is the current in the primary coil?
3. A galvanometer of resistance 120Ω a full scale deflection with a current of $0.0005A$. How would you convert it to an ammeter that reads a maximum current of $5A$?
4. A proton with speed v perpendicular to a magnetic field B is experiences a force F . If the speed of the proton is doubled, the new force is

Solution:

1. The voltmeter reads the average voltage, which is $\sqrt{2}$ times smaller than the maximum voltage of source. So the instantaneous voltage is given by the expression

$$V(t) = 240\sqrt{2}V \cdot \cos(2\pi \cdot 60\text{Hz} \cdot t) = 240\sqrt{2}V \cdot \cos(120\pi \cdot s^{-1} \cdot t)$$

2. According to the ideal transformer identity

$$\frac{V_P}{V_S} = \frac{I_S}{I_P} = a,$$

where V_S and I_S – are voltage and current in the secondary coil, V_P and I_P – are voltage and current in the primary coil, and $1:20 = 1:a$.

So the voltage in the secondary coil is

$$V_S = a \cdot V_P = 20 \cdot 240V = 4800V$$

The current in the secondary coil is

$$I_S = \frac{V_S}{R} = \frac{4800V}{6\Omega} = 800A$$

The current in the primary coil is

$$I_P = \frac{I_S}{a} = \frac{800A}{20} = 40A$$

3. To convert a galvanometer to ammeter we should add to it some parallel resistance R . Since the galvanometer and the resistance R are parallel, the voltage across this parallel connection is equal to the voltage across the galvanometer, which is

$$V_G = 120\Omega \cdot 0.0005A = 0.06V$$

The resistance of this parallel connection is

$$R_{\parallel} = \frac{R_G R}{R_G + R}$$

This ammeter should be able to read a maximum current of $5A$, so

$$V_G = R_{\parallel} \cdot 5A$$

$$0.06V = \frac{120\Omega \cdot R}{120\Omega + R} 5A$$

$$R = \frac{7.2}{600 - 0.06} \Omega \approx \frac{7.2}{600} \Omega = 12\text{m}\Omega$$

4. The Lorentz force, acting on the proton moving with speed v is

$$F = e \cdot v \cdot B$$

The Lorentz force, acting on the proton moving with speed $2v$ is

$$F' = e \cdot 2v \cdot B$$

So

$$\frac{F'}{F} = \frac{e \cdot 2v \cdot B}{e \cdot v \cdot B} = 2 \Rightarrow F' = 2F$$

Answer:

1. $V(t) = 240\sqrt{2}V \cdot \cos(120\pi \cdot s^{-1} \cdot t)$
2. 40A
3. 12m Ω
4. 2F