

A time varying magnetic field $B(t) = B_0 \cos \omega t$

is

pointing out of the page fills the region enclosed by a circle of radius a shown in the figure below.

Determine the induced electric field.

Solution.

We are going to calculate the electric field straight on the edge of the circle with radius r . We right down the Faraday's law:

$$\oint \vec{E} \cdot \vec{l} = \frac{d}{dt} \int \vec{B} \cdot d\vec{A}$$

Now we evaluate the path integral, which is rather simple due to the radial symmetry:

$$\oint \vec{E} \cdot \vec{l} = 2\pi E r$$

The change of the flux:

$$\frac{d}{dt} \int \vec{B} \cdot d\vec{A} = |dB/dt| \pi r^2$$

We combine E and B and obtain

$$E = \left| \frac{dB(t)}{dt} \right| \cdot \frac{r}{2} = B_0 \omega |\sin(\omega t)| \cdot \frac{r}{2}$$

Answer.

$$E = B_0 \omega |\sin(\omega t)| \cdot \frac{r}{2}$$