

A man weighs 750 N on the surface of the Earth. What would be his weight when standing on the Moon? The masses of the earth and the moon are respectively, 5.98×10^{24} kg and 7.36×10^{22} kg. Their radii are respectively 6.37×10^3 km and 1.74×10^3 km.

- 200.5 N
- 123.7 N
- 550.4 N
- 1000.0 N

Solution.

With an application of the universal gravitation law, for a man on the Earth surface one have:

$$F_E = G \frac{m M_E}{R_E^2},$$

and, similarly, in case of Moon:

$$F_M = G \frac{m M_M}{R_M^2},$$

where G is the is the gravitational constant, m is the mass of a man, R and M are the radii and masses of the Earth and the Moon. To evaluate weight on the Moon surface, we will find a proportionality coefficient between forces F_E and F_M . Combining previous two equations, we find

$$F_M = F_E \frac{M_M R_E^2}{M_E R_M^2} = \alpha F_E$$

Than we calculate dimensionless coefficient α numerically:

$$\alpha = \frac{7.36 \times 10^{22} \text{ kg} (6.37 \times 10^3 \text{ km})^2}{5.98 \times 10^{24} \text{ kg} (1.74 \times 10^3 \text{ km})^2} = 0.165,$$

what means that weight on the Moon surface reaches only 16.5% of the weight on the Earth. Now we find corresponding weights of different objects multiplying their weights F_E to α .

Answer.

$$750.0 \text{ N} \times 0.165 = 123.8 \text{ N}$$

$$200.5 \text{ N} \times 0.165 = 33.1 \text{ N}$$

$$123.7 \text{ N} \times 0.165 = 20.4 \text{ N}$$

$$550.4 \text{ N} \times 0.165 = 90.8 \text{ N}$$

$$1000.0 \text{ N} \times 0.165 = 165 \text{ N}$$