

Answer on Question #49017 – Physics – Mechanics | Kinematics | Dynamics

1. A 14 g block of metal ($C_s = 126$) heated to 78 is plunged into 405 g of water at 24 degree C. What is the equilibrium temperature? C_s of water is 4190 Jkg⁻¹K⁻¹. Give your answer to 1 decimal place.

$$m_1 = 0.014 \text{ kg}$$

$$T_1 = 351.1 \text{ K}$$

$$c_1 = 126 \frac{\text{J}}{\text{kg} \cdot \text{K}}$$

$$m_2 = 0.405 \text{ kg}$$

$$T_2 = 297.1 \text{ K}$$

$$c_2 = 4190 \frac{\text{J}}{\text{kg} \cdot \text{K}}$$

$$T = ?$$

Solution.

The metal block will be cooled, while the cold water will be heated. We can write the heat balance equation:

$$m_1 c_1 (T_1 - T) = m_2 c_2 (T - T_2).$$

Here, c_1 and c_2 are specific heat of metal and water, respectively.

One can find the final temperature:

$$T = \frac{m_1 c_1 T_1 - m_2 c_2 T_2}{m_1 c_1 - m_2 c_2}$$

Let check the dimension: $[T] = \frac{\text{kg} \cdot \frac{\text{J}}{\text{kg} \cdot \text{K}} \cdot \text{K}}{\text{kg} \cdot \frac{\text{J}}{\text{kg} \cdot \text{K}}} = \text{K}.$

Let evaluate the quantity:

$$T = \frac{0.014 \cdot 126 \cdot 351.1 - 0.405 \cdot 4190 \cdot 297.1}{0.014 \cdot 126 - 0.405 \cdot 4190} = 297.0 (\text{K}) = 23.9 (^\circ \text{C}).$$

Answer: 23.9 °C .