Answer on Question #47650 - Physics - Other

Question.

A mass of 0.50 kg is hung from a spring and has a frequency of oscillation of 0.113 Hz. What is the spring constant? The mass is replaced with a second unknown mass and the frequency of oscillation is found to be 0.171 Hz. What is the unknown mass?

Given:

$$m_0 = 0.5 \, kg$$

$$v_0 = 0.113 \; Hz$$

$$\nu = 0.171 \, Hz$$

Find:

$$k = ?$$

$$m = ?$$

Solution.

By definition the period of a harmonic oscillator can be approximated by the following formula:

$$T_0 = 2\pi \sqrt{\frac{m_0}{k}}$$

And we know that

$$v_0 = \frac{1}{T_0} = \frac{1}{2\pi} \sqrt{\frac{k}{m_0}}$$

Therefore,

$$k = 4\pi^2 v_0^2 m_0$$

But *k* is constant, so:

$$k = 4\pi^2 v_0^2 m_0 = 4\pi^2 v^2 m \to m = m_0 \left(\frac{v_0}{v}\right)^2$$

Calculate:

$$k = 4\pi^2 \cdot 0.113^2 \cdot 0.5 = 0.252 \frac{N}{m}$$

$$m = 0.5 \left(\frac{0.113}{0.171}\right)^2 = 0.218 \, kg$$

Answer.

$$k = 4\pi^2 {v_0}^2 m_0 = 0.252 \; \frac{N}{m}$$

$$m = m_0 \left(\frac{v_0}{v}\right)^2 = 0.218 \, kg$$

http://www.AssignmentExpert.com/