

Answer on Question #46640, Physics, Mechanics | Kinematics | Dynamics

Question:

a body takes time t to reach the bottom of an inclined plane of angle with horizontal. if plane is rough time taken is $2t$. what is the coefficient of friction of rough surface.

Answer:

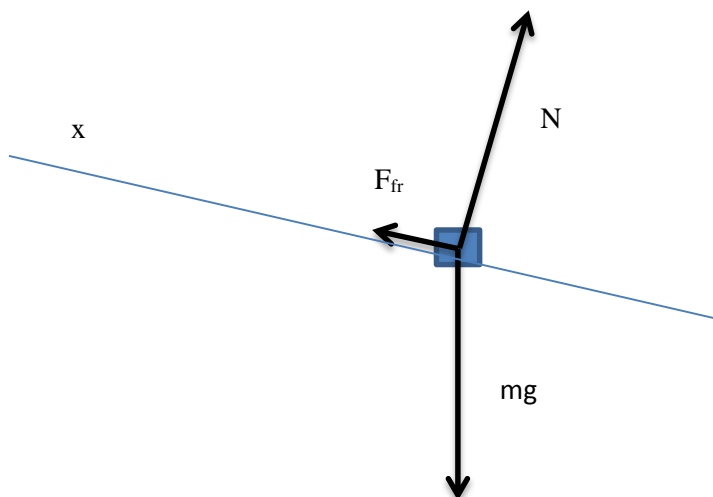
Suppose length of plane equals l :

$$l = \frac{at^2}{2}$$

Therefore:

$$t = \sqrt{\frac{2l}{a}}$$

In case with friction we have:



Newton's laws of motion:

$$x: \quad ma = mg \sin \theta - F_{fr}$$

$$y: \quad N = mg \cos \theta$$

Friction force equals $F_{fr} = \mu N = \mu mg \cos \theta$, μ - coefficient of friction.

Therefore:

$$a_2 = g \sin \theta - \mu g \cos \theta$$

In first case $\mu = 0$:

$$a_1 = g \sin \theta$$

Therefore:

$$t_1 = t = \sqrt{\frac{2l}{g \sin \theta}}$$

$$t_2 = 2t = \sqrt{\frac{2l}{(g \sin \theta - \mu g \cos \theta)}}$$

$$g \sin \theta = 4 \cdot (g \sin \theta - \mu g \cos \theta)$$

$$\mu = 3 \tan \theta$$

Answer: $\mu = 3 \tan \theta$