## Problem.

What is the probability that a donor atom at energy ED is ionized ?

## Solution:

There are three possible states of the system that consist of a single donor atom:

- one ionized state with no electron;
- two unionized states (either spin-up or spin-down).

If $I$ is the ionization energy, then the Gibbs factors of these states are

- ionized state $\exp (0)=1(\varepsilon=0, n=0)$;
- unionized state $\exp \left(-\frac{-I-\mu}{k T}\right)=\exp \left(\frac{I+\mu}{k T}\right)$.

Hence the probability equals $\frac{1}{1+2 \exp \left(\frac{I+\mu}{k T}\right)}$.

