A charged particle of mass m is released from rest x along electric field e.j^ (vector) find angular momentum of particle from origin

Solution :

Distinguish three axes x,y,z they correspond to the three vectors $x: \bar{i}, y: \bar{j}, z: \bar{k}$

Then particle has {x,0,0} coordinates, and field $\overline{E} = \{0, e, 0\}$

Impulse (momentum) from Newton's second law :

$$\frac{d\bar{p}}{dt} = \bar{F} = q\bar{E} = q*\bar{J}*e$$

Obvious that $\bar{p} = qet * \bar{j}$

From angular momentum (L)definition:

 $\bar{L} = [\bar{r} * \bar{p}] = (x * \bar{\iota} + y * \bar{j} + z * \bar{k}) * (qet * \bar{j}) \text{ (cross vector product)}$

But z always equal to zero, because there is no force in z direction.

$$\bar{L} = (x * \bar{\iota} + y * \bar{j}) * (qet * \bar{j}) = qet * (x * \bar{\iota} + y\bar{j}) * \bar{j} = qetx * \bar{k}$$

 $\bar{j} * \bar{j} = 0$ (cross vector product)