Answer on Question #43667 - Physics - Mechanics | Kinematics | Dynamics

Two trains start at the same time from Delhi and Jalandhar, distance of 400 km, travelling, one at the rate of 48 km/hr and the other at 72 km/hr. Where will they meet and in what time from starting.

Solution:

$$\begin{split} S &= 400 \text{ km} - \text{distance between two trains;} \\ V_1 &= 48 \frac{\text{km}}{\text{hr}} - \text{velocity of the first train;} \\ V_2 &= 72 \frac{\text{km}}{\text{hr}} - \text{velocity of the first train;} \end{split}$$

Let trains are moving towards and the distance travelled by the train with slower speed be x. Accordingly the distance travelled by the faster train will be y=S-x. Let the time taken by the trains to travel the distance be t

According to question:

first (slower)train:
$$t = \frac{x}{V_1}$$
 (1)
second (faster)train: $t = \frac{y}{V_2} = \frac{S - x}{V_2}$ (2)
(1) = (2):

$$\frac{x}{V_1} = \frac{S - x}{V_2}$$

$$V_2x = SV_1 - V_1x$$

$$x(V_1 + V_2) = SV_1$$

$$x = \frac{SV_1}{V_1 + V_2} = \frac{400 \text{km} \cdot 48 \frac{\text{km}}{\text{hr}}}{48 \frac{\text{km}}{\text{hr}} + 72 \frac{\text{km}}{\text{hr}}} = 160 \text{ km}$$

$$y = S - x = 400 \text{km} - 160 \text{ km} = 240 \text{ km}$$

$$t = \frac{x}{V_1} = \frac{160 \text{ km}}{48 \frac{\text{km}}{\text{hr}}} = 3 \text{ hours 20 minutes}$$

Answer: trains will meet 160 km from station where slower train has been started to move; they will meet after 3 hours 20 minutes.