

Answer on Question #43497 – Physics - Mechanics | Kinematics | Dynamics | for completion

A boy throws a ball vertically upwards with a velocity of 25 m/s while he was standing on a cliff. On the way down it just misses the thrower and falls down on the ground if the height of the building was 49 m. Determine

- a) the total time of flight?
- b) the velocity with which it reaches the ground?

Solution:

$$V = 25 \frac{m}{s} \text{ - initial velocity of the ball;}$$

$$h = 49m \text{ - height of the building;}$$

Equation of motion for the ball along the Y-axis:

$$y: h = -Vt + \frac{gt^2}{2}$$
$$gt^2 - Vt - 2h = 0$$

We have a quadratic equation (t-total time of flight), and we take only positive root of the equation (time t can not be negative):

$$t = \frac{V + \sqrt{V^2 + 8gh}}{2g} = \frac{25 \frac{m}{s} + \sqrt{\left(25 \frac{m}{s}\right)^2 + 8 \cdot 9.8 \frac{m}{s^2} \cdot 49m}}{2 \cdot 9.8 \frac{m}{s^2}} = 28.4 \text{ s}$$

Rate equation for the ball along Y-axis (V_{final} -final velocity of the ball):

$$V_{final} = -V + gt = -25 \frac{m}{s} + 9.8 \frac{m}{s^2} \cdot 28.4 \text{ s} = 253 \frac{m}{s}$$

Answer: a) 28.4 s

b) $253 \frac{m}{s}$

