

Answer on Question # 42896, Physics, Other

Task:

32. For a damped harmonic oscillator of mass 200 gm, the values of spring constant and damping constant are, respectively, 90 N/m and 0.04 kg/s. The time taken for its amplitude of vibration to drop to half of its initial values ($\log_e 2 = 0.693$):

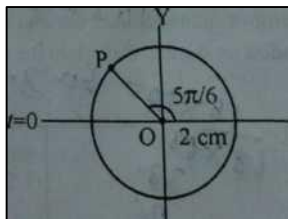
- (a) 7.0 s
- (b) 14.2 s
- (c) 15.9 s
- (d) 26.6 s

Solution:

$$\ln \frac{A_1}{A_2} = \frac{A_0 e^{-\beta t}}{A_0 e^{-\beta(t+\Delta t)}} = \ln 2 = 0.693 = \beta \Delta t = \frac{\lambda}{T} \Delta t \Rightarrow \Delta t = \frac{\ln 2 \cdot T}{\lambda} = \frac{\ln 2 \cdot 2\pi \sqrt{\frac{m}{k}}}{\lambda} \approx 7.0s$$

Answer: (a) 7.0 s

33. For the following reference circle, the equation for simple harmonic motion (S.H.M.) is:



- (a) $x = -2\sin(2\pi t + \pi/4)$
- (b) $x = -2\sin(3t + \pi/3)$
- (c) $x = -2\cos(\pi/6 - t)$
- (d) $x = -2\cos \pi t$

Answer: (b) $x = -2\sin(3t + \pi/3)$

