

Answer on Question #42194, Physics, Mechanics | Kinematics | Dynamics

3. A rock is dropped (from rest) from the top of a 60 m tall building. How far above the ground is the rock 1.2 s before it reaches the ground?

4. A mother racing her son has half the kinetic energy of the son, who has half the mass as the mother. Mother speeds up by 1.0 m/s and then has the same kinetic energy as that of the son. What are the original speeds of the mother and the son?

Solution:

3.

Given:

$$y_0 = 60 \text{ m},$$

$$t = 1.2 \text{ s},$$

$$y_1 = ?$$

An object in free fall experiences an acceleration g of -9.81 m/s^2 . (The - sign indicates a downward acceleration.) Whether explicitly stated or not, the value of the acceleration in the kinematic equations is -9.81 m/s^2 for any freely falling object.

The equation of moving to the top point is

$$y = y_0 + v_0 t + \frac{1}{2} a t^2$$

where

$y_0 = 60 \text{ m}$ is initial position

$v_0 = 0$ is initial speed

$a = g = -9.81 \text{ m/s}^2$ is acceleration

At time $t = 1.2 \text{ s}$, the position of a rock is

$$y_1 = 60 + 0 + \frac{1}{2} (-9.81) 1.2^2 = 52.94 \text{ m}$$

Answer. $y_1 = 52.94 \text{ m}$.

4. A mother racing her son has half the kinetic energy of the son, who has half the mass as the mother. Mother speeds up by 1.0 m/s and then has the same kinetic energy as that of the son. What are the original speeds of the mother and the son?

Solution:

Given:

$$m_2 = m_1/2,$$

$$KE_1 = KE_2/2$$

$$v_1 = ?,$$

$$v_2 = ?$$

The kinetic energy is

$$\begin{aligned} KE_1 &= \frac{KE_2}{2} \\ \frac{m_1 v_1^2}{2} &= \frac{m_2 v_2^2}{4} \end{aligned}$$

So,

$$\begin{aligned} 2m_1 v_1^2 &= m_2 v_2^2 \\ m_2 &= m_1/2 \end{aligned}$$

Thus,

$$2m_1 v_1^2 = \frac{m_1}{2} v_2^2$$

$$4v_1^2 = v_2^2 \quad (1)$$

From given we also have

$$\begin{aligned} \frac{m_1(v_1 + 1)^2}{2} &= \frac{m_2 v_2^2}{2} \\ \frac{m_1(v_1 + 1)^2}{2} &= \frac{m_1 v_2^2}{4} \end{aligned}$$

Thus, the second equation is

$$2(v_1 + 1)^2 = v_2^2 \quad (2)$$

$$\begin{aligned} 2(v_1 + 1)^2 &= 4v_1^2 \\ 2(v_1^2 + 2v_1 + 1) &= 4v_1^2 \end{aligned}$$

We obtain quadratic equation

$$2v_1^2 - 2v_1 - 1 = 0$$

Solution is

$$v_1 = \frac{2 + \sqrt{4 + 4 \cdot 2}}{4} = 1.366 \text{ m/s}$$

$$v_2 = 2v_1 = 2 \cdot 1.366 = 2.732 \text{ m/s}$$

Answer. The mother speed is $v_1 = 1.366 \text{ m/s}$,

the son speed is $v_2 = 2.732 \text{ m/s}$