

Answer on Question #41998, Physics, Other

A pendulum takes 3 minutes to complete 350 swings. What is the length of the pendulum?

Solution:

Given:

$$t = 3 \text{ min} = 180 \text{ s},$$

$$N = 350 \text{ swings},$$

$$L = ?$$

A simple pendulum is one which can be considered to be a point mass suspended from a string or rod of negligible mass. For small amplitudes, the period (amount of time it takes for the pendulum to complete one swing) of such a pendulum can be approximated by:

$$T = 2\pi \sqrt{\frac{L}{g}}$$

where L is pendulum length and $g = 9.81 \text{ m/s}^2$ is acceleration of gravity

From given data we have that

$$T = \frac{t}{N}$$

Thus,

$$\begin{aligned} 2\pi \sqrt{\frac{L}{g}} &= \frac{t}{N} \\ L &= g \left(\frac{t}{2\pi N} \right)^2 \\ L &= 9.81 \cdot \left(\frac{180}{2 \cdot 3.14159 \cdot 350} \right)^2 = 0.0657 \approx 0.066 \text{ m} \end{aligned}$$

Answer. $L = 0.066 \text{ m} = 6.6 \text{ cm.}$