Answer on Question #40810, Physics, Mechanics

A 2 kg and a 4 kg hang freely at opposite ends of a light inextensible string which passes over a small, light pulley fixed onto a rigid support. Calculate the acceleration of the system.

Solution:



Given:

$$\begin{split} m_1 &= 4 \text{ kg}, \\ m_2 &= 2 \text{ kg}, \\ W_1 &= m_1 g \\ W_1 &= m_2 g \end{split}$$

The equations of motion are:

$$m_1 a = m_1 g - T$$
$$m_2 a = T - m_2 g$$

The adding of two equations gives:

$$m_1a + m_2a = m_1g - T + T - m_2g$$

$$m_1a + m_2a = m_1g - m_2g = g(m_1 - m_2)$$

Thus, the acceleration is

$$a = \frac{g(m_1 - m_2)}{m_1 + m_2}$$
$$a = \frac{9.81 \cdot (4 - 2)}{4 + 2} = 3.27 \text{ m/s}^2$$

Answer. $a = 3.27 \text{ m/s}^2$.