

Answer on Question #40446

Physics – Mechanics | Kinematics | Dynamics

Question:

An object is tracked by a radar station and found to have a position vector by $\mathbf{r} = (3500 - 160t)\mathbf{i} + 2700\mathbf{j} + 300\mathbf{k}$, with \mathbf{r} in m and t in sec. The radar station's x-axis points east, its y-axis north and its z-axis vertically up. If the object is a 250-kg missile warhead, what are (a) its linear momentum (b) its direction of motion (c) its net force on it.

Solution:

The linear momentum is

$$\vec{p} = m\vec{v},$$

where $m = 250 \text{ kg}$ is mass of the object and \mathbf{v} is its velocity.

$$\vec{v} = \frac{d\vec{r}}{dt} = -160\mathbf{i}.$$

Thus,

$$\vec{p} = -160m\mathbf{i} = -40,000\mathbf{i} \frac{\text{kg} \cdot \text{m}}{\text{s}}.$$

Because only the X coordinate of the object is changed in time and X axis points East, the object moves to the East.

The net force $F_{net} = ma$ acting on the object is zero, because the acceleration

$$\mathbf{a} = \frac{d\vec{v}}{dt} = \frac{d^2\vec{r}}{dt^2} = 0.$$

Answer:

a) $\vec{p} = -40,000\mathbf{i} \frac{\text{kg} \cdot \text{m}}{\text{s}}$

b) East

c) 0.