

Answer on Question #39567 – Physics – Other

Let  $M$  and  $m$  be the masses of Luke and c-3po respectively,  $v$  and  $w$  – velocities of Luke and c-3po after collision.

Darth Vader pushes Luke with 17N. According to the Newton's Second law:

$$F = Ma$$

$$M = \frac{F}{a} = \frac{17N}{\frac{11m}{s^2}} = \frac{17}{11} kg$$

According to the law of conservation of momentum:

$$Mv_0 = Mv + mw$$

where  $v_0$  is the initial velocity of Luke.

Using the law of conservation of momentum:

$$\frac{Mv_0^2}{2} = \frac{Mv^2}{2} + \frac{mw^2}{2}$$

From the first equation we have

$$v = v_0 - \frac{m}{M}w$$

Supstitute it into the second equation:

$$\begin{aligned} \frac{Mv_0^2}{2} &= \frac{M(v_0 - \frac{m}{M}w)^2}{2} + \frac{mw^2}{2} \\ \frac{Mv_0^2}{2} &= \frac{Mv_0^2}{2} - \frac{2Mv_0 \frac{m}{M}w}{2} + \frac{M \frac{m^2}{M^2}w^2}{2} + \frac{mw^2}{2} \\ 0 &= -v_0 mw + \frac{m^2 w^2}{2M} + \frac{mw^2}{2} \end{aligned}$$

Divide the equation by  $m$ :

$$\begin{aligned} 0 &= -v_0 w + \frac{mw^2}{2M} + \frac{w^2}{2} \\ m &= \frac{2M}{w^2} \left( v_0 w - \frac{w^2}{2} \right) \end{aligned}$$

Substitute  $M = \frac{17}{11} kg$ ,  $w = 8m/s$  and  $v_0 = v_0(t) = at = 11t$ :

$$m = \frac{2 \cdot \frac{17}{11}}{64} \left( 11t \cdot 8 - \frac{64}{2} \right) = \frac{17}{11 \cdot 32} (88t - 32) = 4.25t - \frac{17}{32}$$

So the mass of c-3po is  $4.25t - \frac{17}{32}$ . It depends how long (in seconds) Dart Vader applied his force.