

In an experiment to prove the concept of the second condition of equilibrium, a boy balanced the meterstick on a peg board exactly at the midpoint. He then put a cylindrical metal at the 10cm mark and moved the meterstick to balance it again. If the meterstick weighs 12g, how much does the cylindrical metal weigh?

Solution:

$L = 1m$ – length of the meterstick;

$m_1 = 12g$ – weight of the meterstick;

m_2 – weight of the cylindrical metal;

$d = 10cm$ – distance from the end of meterstick to the cylindrical metal;

x – displacement of the meterstick;

Second condition of equilibrium (point A):

$$A: M_1 + M_2 = 0 \quad (1)$$

$$M_1 = m_1 g \cdot \left(\frac{L}{2} - x - d \right) \quad (2)$$

$$M_2 = -m_2 g \cdot \left(\frac{L}{2} + x \right) \quad (3)$$

(3) and (2) in (1):

$$m_1 g \cdot \left(\frac{L}{2} - x - d \right) - m_2 g \cdot \left(\frac{L}{2} + x \right) = 0$$

$$m_2 = m_1 \cdot \frac{\frac{L}{2} - x - d}{\frac{L}{2} + x} = m_1 \cdot \frac{L - 2x - 2d}{L + 2x} = 12g \cdot \frac{100cm - 2x - 20cm}{100cm + 2x}$$

$$= 12g \cdot \frac{80cm - 2x}{100cm + 2x}$$

Hence, to find m_2 we need to know the displacement of the meterstick (x)

Answer: to find m_2 we need to know the displacement of the meterstick, formula for the m_2 :

$$m_2 = 12g \cdot \frac{80cm - 2x}{100cm + 2x}$$