

A roller-coaster car is moving at 20 m/s along a straight horizontal track. What will its speed be after climbing the 15-m hill shown in the figure, if friction is ignored?

Solution:

Conservation of energy:

$$W_{\text{kinetic start}} + W_{\text{potential start}} = W_{\text{kinetic top}} + W_{\text{potential at top}}$$

let's call the level of the horizontal track our reference level, so potential energy will be zero there, so we have:

$$\begin{aligned}\frac{mV_{\text{start}}^2}{2} &= \frac{mV_{\text{top}}^2}{2} + mgh \\ V_{\text{top}}^2 &= V_{\text{start}}^2 - 2gh \\ V_{\text{top}} &= \sqrt{V_{\text{start}}^2 - 2gh} = \sqrt{\left(20 \frac{\text{m}}{\text{s}}\right)^2 - 2 \cdot 9.8 \frac{\text{m}}{\text{s}^2} \cdot 15\text{m}} = 10.3 \frac{\text{m}}{\text{s}}\end{aligned}$$

Answer: speed of the car will be $10.3 \frac{\text{m}}{\text{s}}$.