

A 1600 kg car moves along a horizontal road at speed $v_0 = 17.3 \text{ m/s}$. The road is wet, so the static friction coefficient between the tires and the road is only $\mu_s = 0.311$ and the kinetic friction coefficient is even lower, $\mu_k = 0.2177$.

The acceleration of gravity is 9.8 m/s^2 . Assume: No aerodynamic forces; $g = 9.8 \text{ m/s}^2$, forward is the positive direction.

What is the highest possible deceleration of the car under such conditions?

Answer in units of m/s^2

Solution:

$m = 1600 \text{ kg}$ – mass of the car;

$V_0 = 17.7 \frac{\text{m}}{\text{s}}$ – speed of the car;

$g = 9.8 \frac{\text{m}}{\text{s}^2}$ – acceleration due to gravity;

a_{max} – highest possible deceleration of the car

$\mu_s = 0.311$ – static friction coefficient between the tires and the road ;

$\mu_k = 0.2177$ – kinetic friction coefficient ;

Second Newton's law for the car (N - reaction force):

y: $N = mg$

x: $F_{\text{fr}} = ma_{\text{max}}$ (1)

Formula for the friction force:

$F_{\text{fr}} = N\mu_k = mg\mu_k$ (2) (we use μ_k because car moves)

(2)in(1):

$mg\mu_k = ma_{\text{max}}$

$a_{\text{max}} = g\mu_k = 9.8 \frac{\text{m}}{\text{s}^2} \cdot 0.2177 = 2.13 \frac{\text{m}}{\text{s}^2}$

Answer: the highest possible deceleration of the car under such conditions is $2.13 \frac{\text{m}}{\text{s}^2}$.